

## X-ray systems and on-line optimization

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## Introduction

Zumbach Electronic AG

The RAYEX<sup>®</sup> S measurement system

The RAYEX<sup>®</sup> S model

The Kalman filter

The IEFK for RAYEX<sup>®</sup> S

Implementation issues

# Mathematics and industrial applications

Applied mathematics becomes increasingly important

- ▶ digital control (flexibility during operation, flexibility for modifications, more complex controllers realizable, lower price)
- ▶ image processing (new applications, on-line processing)
- ▶ estimation of quantities, measurement (on-line processing, faster processing, more complex modelling)
- ▶ optimization in logistics (big data processing)

# Drivers for mathematics in industry

- ▶ Increasing computing power
- ▶ Sophisticated hardware programming capabilities (FPGA, HW/SW-codesign)
- ▶ Simulation techniques, methods and tools
- ▶ Rapid control prototyping techniques and tools (code generation)

# Mathematics is becoming important for SMEs

- ▶ Evolution from Mechanics, through Electronics and Software to Mathematics
- ▶ Basic disciplines are still needed, but focus shifts
- ▶ Computing platforms, sensors, actuators, become commodities, mathematics gives the individual “touch” (competitive advantage).
- ▶ Impact is relevant not only for big companies, but even (or maybe in particular) for SMEs

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## Zumbach In Numbers

Swiss Quality Precision Engineering At Your Disposal

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For nearly **60** years in the world market

Worldwide **11** own companies

Worldwide more than **40** sales and service stations

More than **200** employees

**8** different measurement technologies for best results

Worldwide, more than **100'000** running systems

# Worldwide Customer Service

Always Close To You Wherever You Are





- Leading manufacturer of in-line measuring, monitoring and control systems
- Pioneer in in-line measurement systems, based on various technologies
- Large number of international patents and trademarks
- Manufacturing and R&D centers in Switzerland and the US
- Expert sales and customer support from international subsidiaries with fully equipped service and spare part facilities
- Platform [blog.zumbach.com](http://blog.zumbach.com) with monthly publications to topics of the on-line measurement

# Partnership With Customers

## Systems Tailored To Different Industries

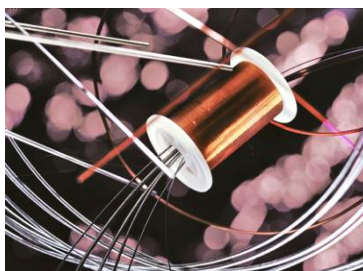
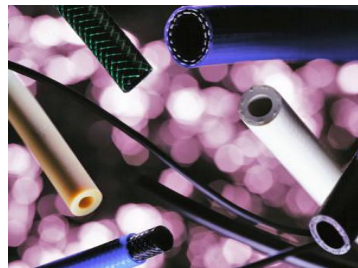
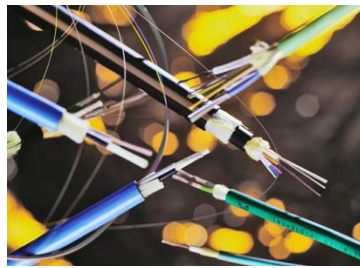
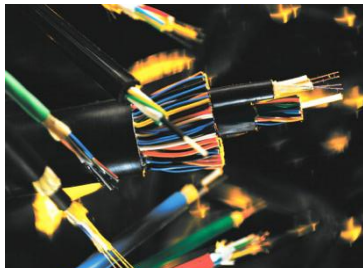
Wire and Cable

Fibre Optic  
and Glass

Plastics and  
rubber

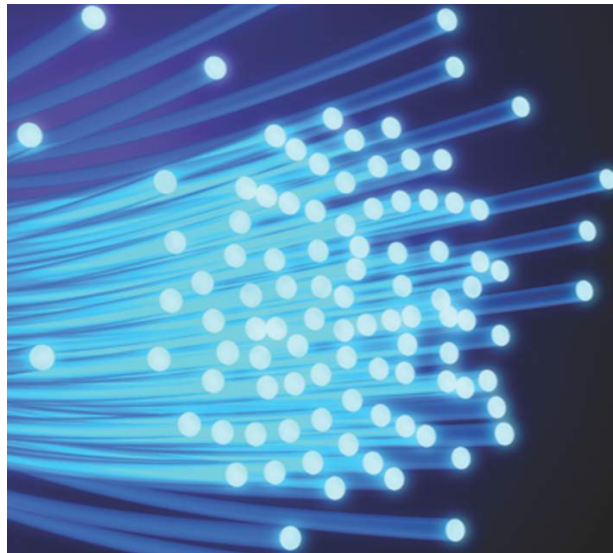
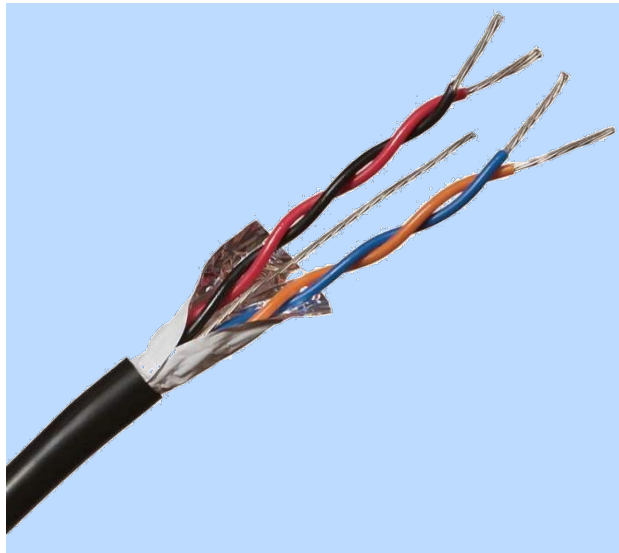
Non-ferrous

Steel and Metal



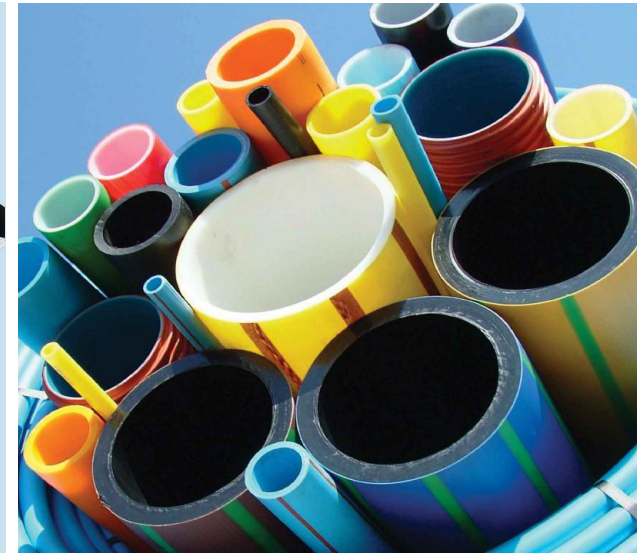
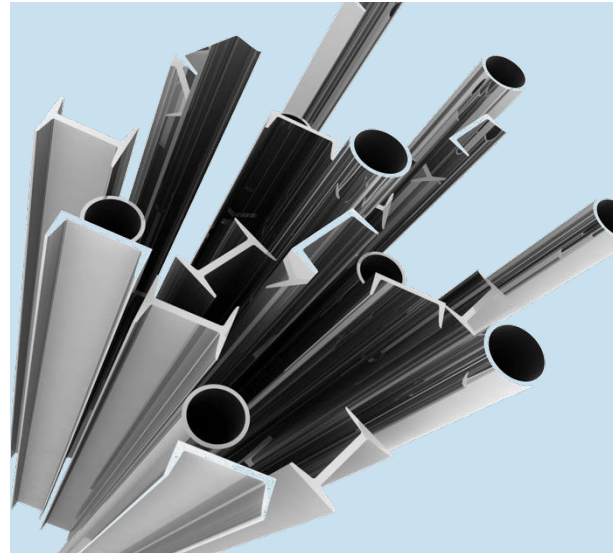
### All extruded Products:

- Telecommunication and data cables
- Fibre optic cables
- Energy and control cables
- Magnet wire
- Fine wire
- Low, Medium, High voltage cables



### All extruded Products:

- Tubing
- Medical tubing / catheters
- Hoses
- Profiles

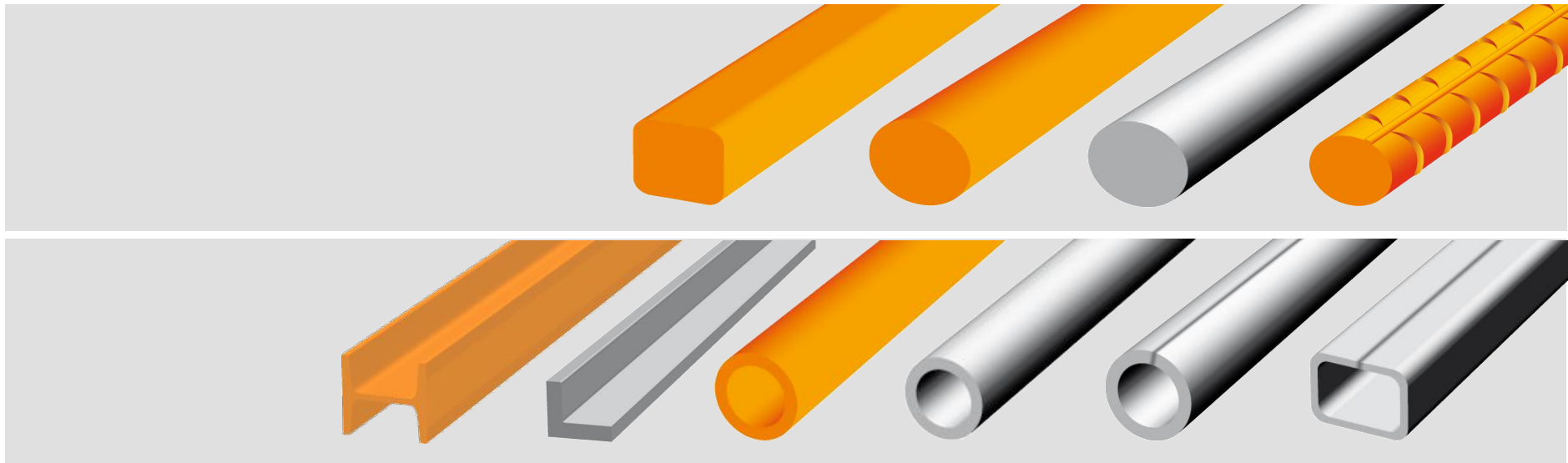


### Hot rolling:

- Bar, rod
- Profiles and seamless pipe
- Welded pipe
- QC (NDT)

### Cold processes such as:

- Peeling
- Grinding
- Bending
- Polishing etc.



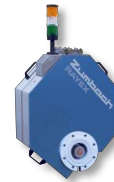
# Technologies – For Each Application The Best Solution

## Trend Setter Of Different Measurement Technologies



### Laser / Optics

Dimension measurement with shadow principle



### X-rays

Cross section measurement (3 layers)



### Ultrasonic

Eccentricity / Wall thickness



### Linear Sensor

(Multi-colour LED sources)  
Diameter / Ovality



### Inductive + Laser

Eccentricity / Diameter / Ovality



### Laser light section technique / Image processing

Profile and shape measurement



### Spark test

Isolation test with high voltage



### Light section technique / Image processing

Quality surface monitoring

# Technologies – For Each Application The Best Solution

## Completing the Product Line of Industrial Equipment



### Capacitance Measuring Systems

Including Fast Fourier Transform / Structural Return Loss Software



### DVW / DVO

Oscillating Measuring Devices for Width/Height and Sector Cables



### LSV

Speed and Length Measurement



### CALIBRATOR SP

Checking Device for periodic Verification and Calibration of Spark Testers



### WST TEMPMASTER

Conductor Preheaters



### Surface Quality

Inspection Systems with Machine Vision / CCD Cameras



### AUTAC

Temperature Control Sensors

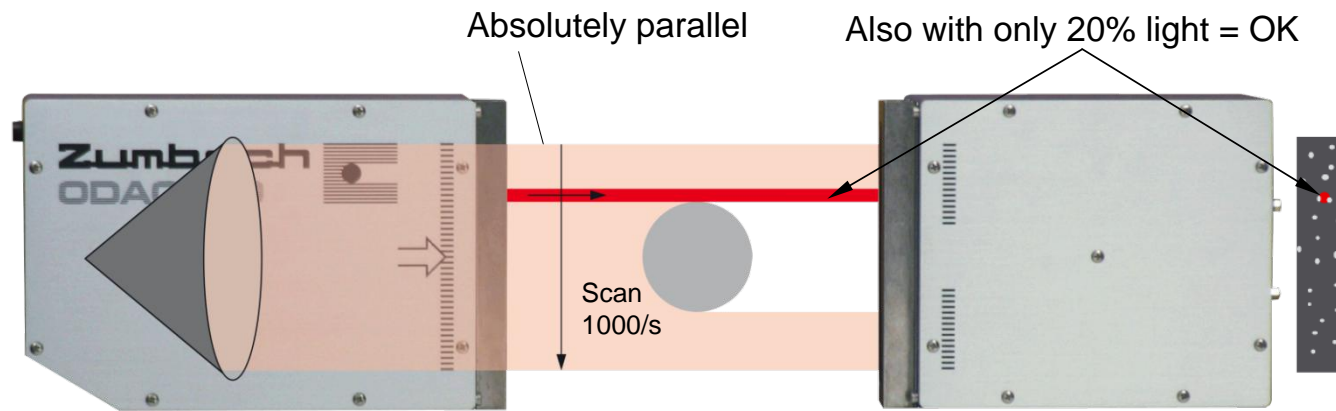


### USYS

Universal Data Acquisition, Processing and Display Units

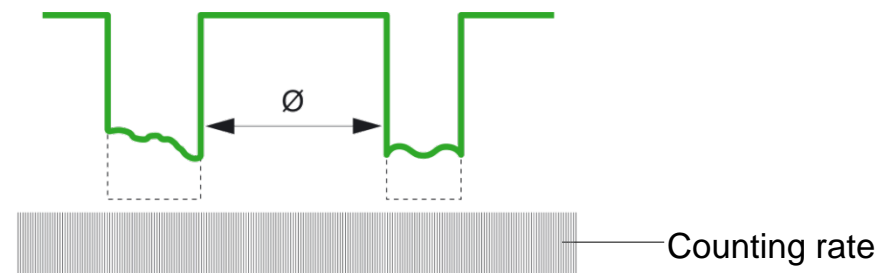
# Laser Scanning Principle

World-wide most used measuring principle



## Measurement

- Very high accuracy (parallel/linear)
- Immune on dirt
- Immune on light variations
- Immune on vertical and horizontal movements

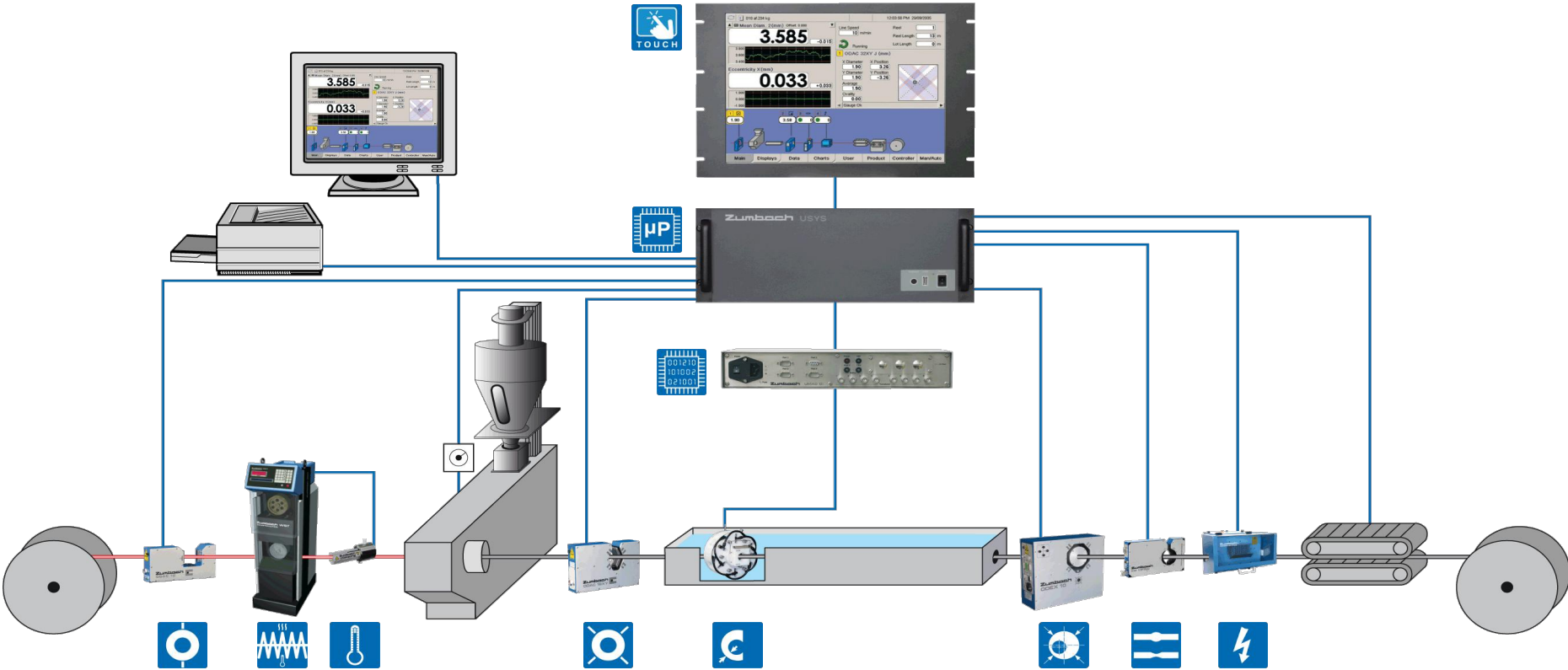


Resolution = 0.0001 mm (.000004 in.)

Rule of thumb for accuracy = 10 x resolution = 0.001 mm (.00004 in.)



# Example of cable Extrusion Line Equipped with Measurement and Control Instruments



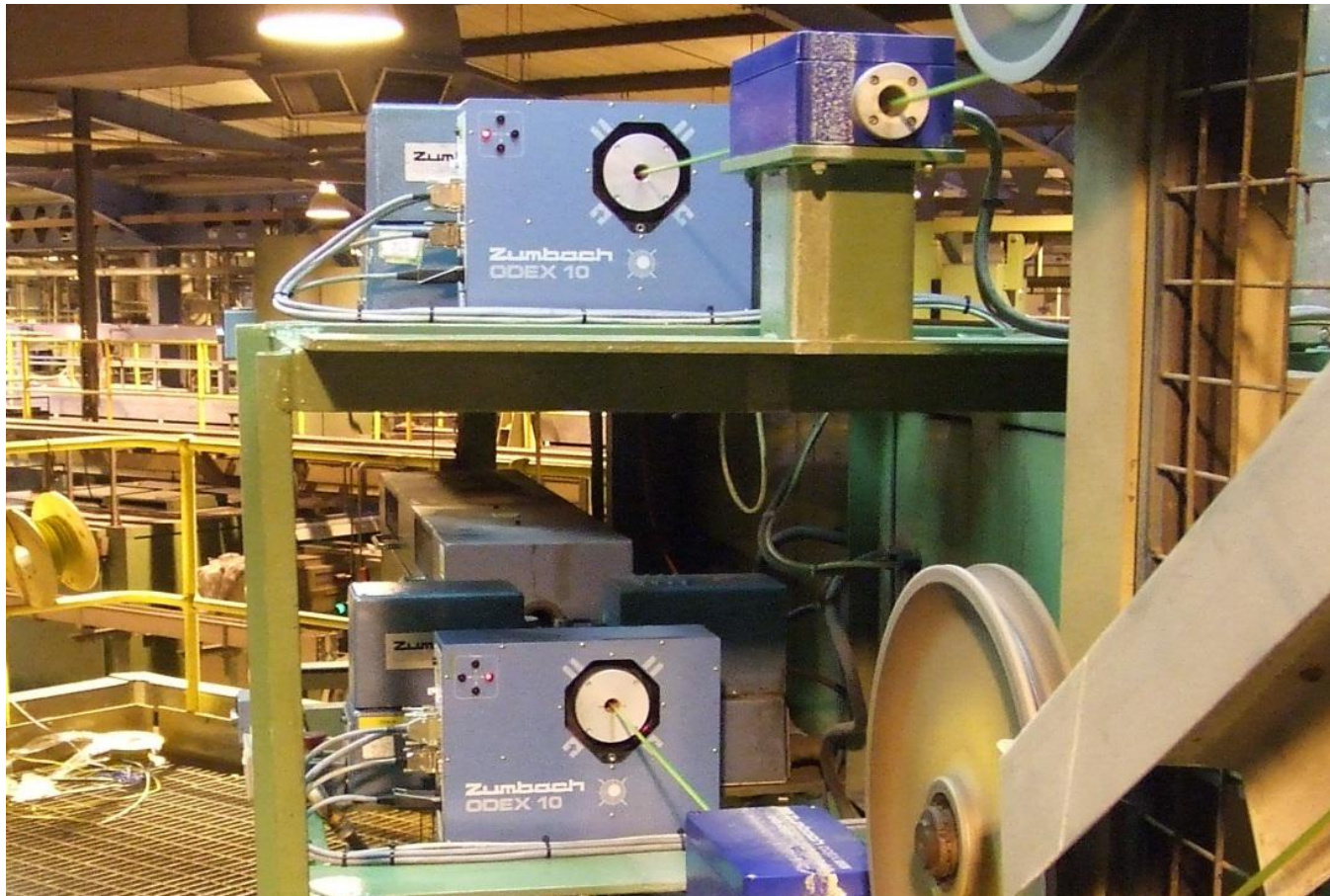
## 2 x ODAC® 152XY-J

Laser-scanning measurement of outside diameter for power cables



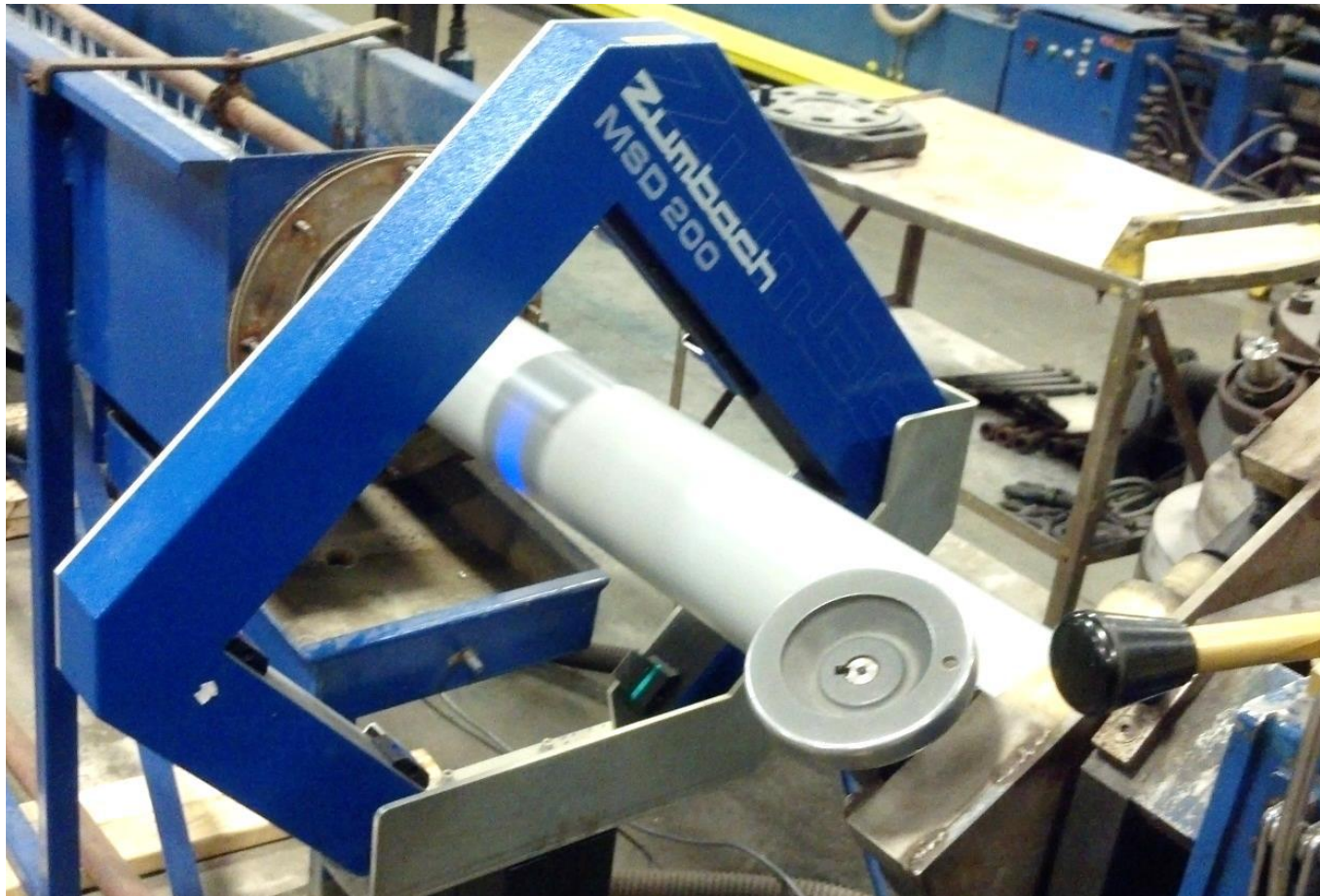
## ODEX® 10

### Eccentricity measurement system for communication cables



## MSD 200

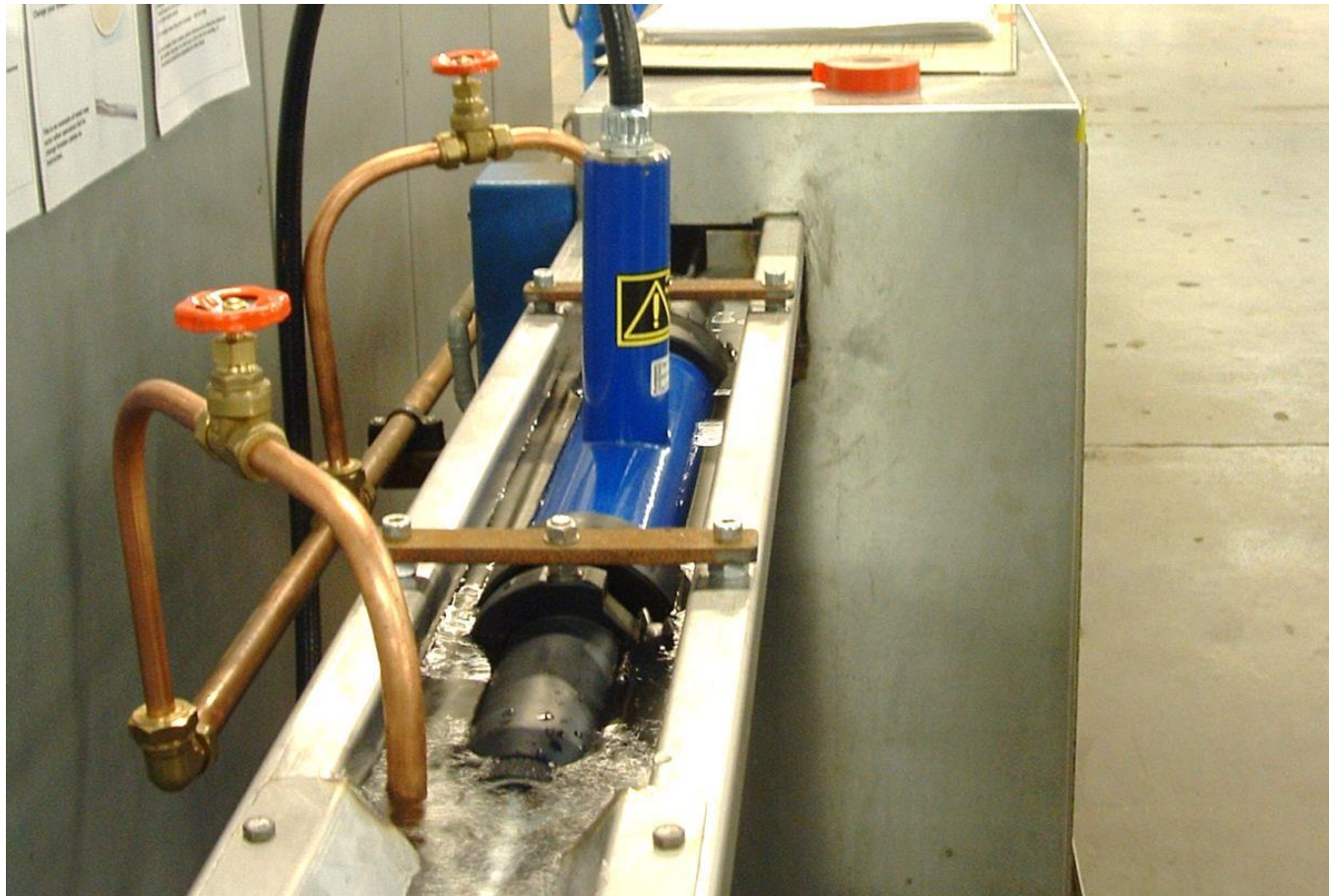
Light shadow-based diameter measurement for tubes



**CAPAC®**

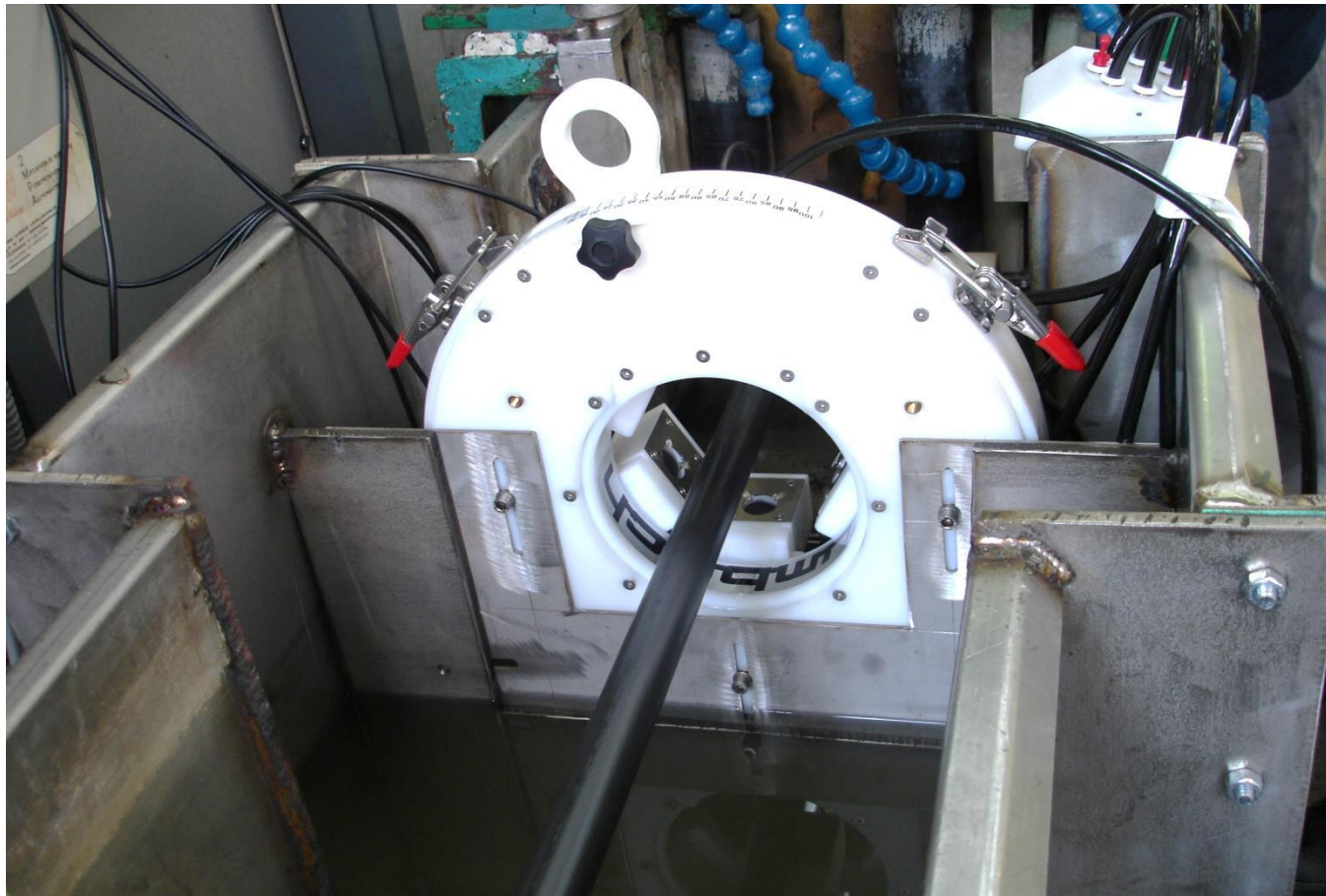
Capacitance measurement for communication cables

**Zumbach**  
SWISS PRIME MEASURING SINCE 1957



## UMAC® Z100-6K

Ultra-sound measurement system for cable layer thickness measurement



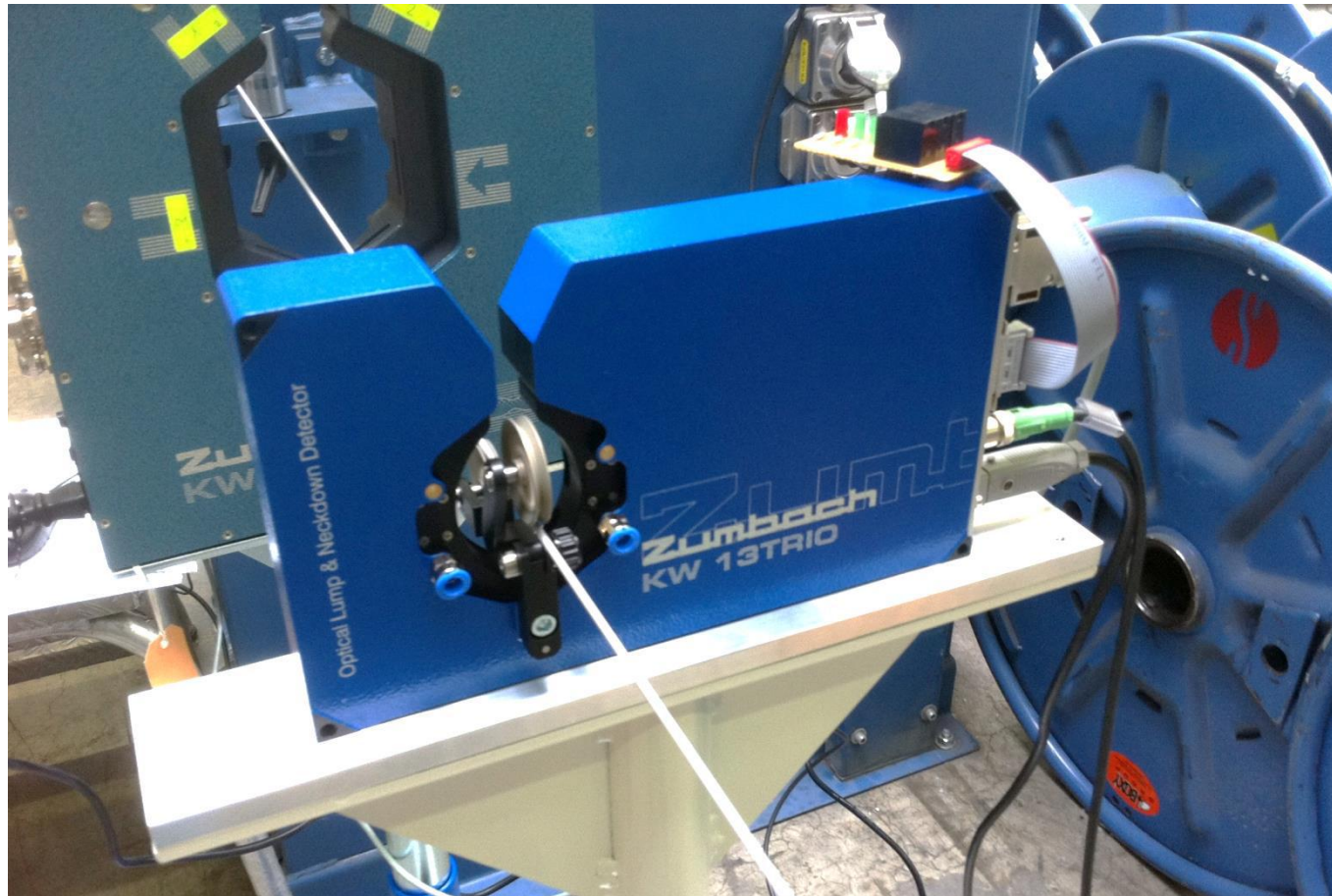
## AST-L 15.50

High-voltage test system for the detection of insulation faults



## KW 13TRIO

Lump and neck detection system for cable defects





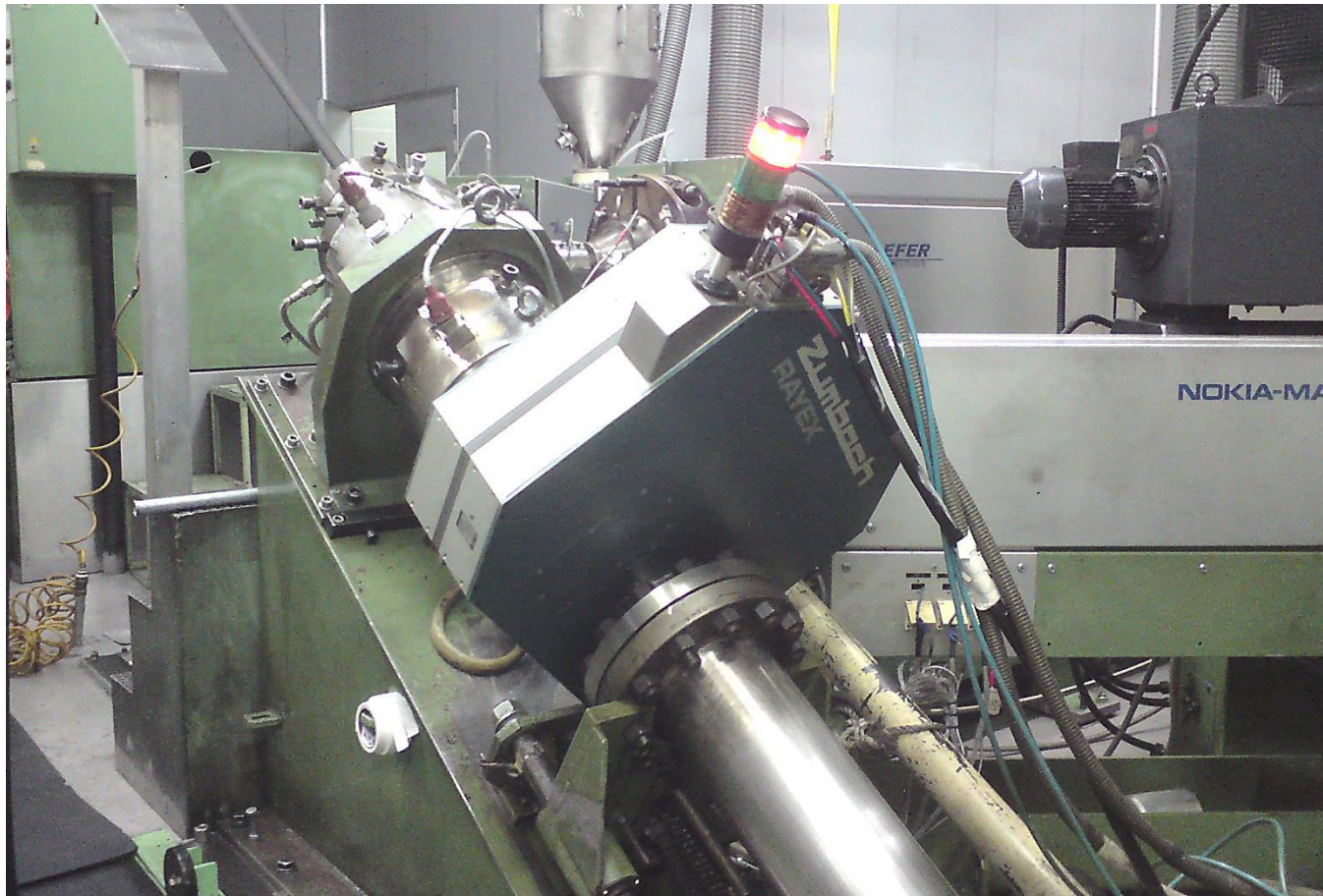
## SIMAC® 63

Surface measurement system for the detection of defects in plastics products



## RAYEX® 220

X-ray measurement system for high-voltage cables



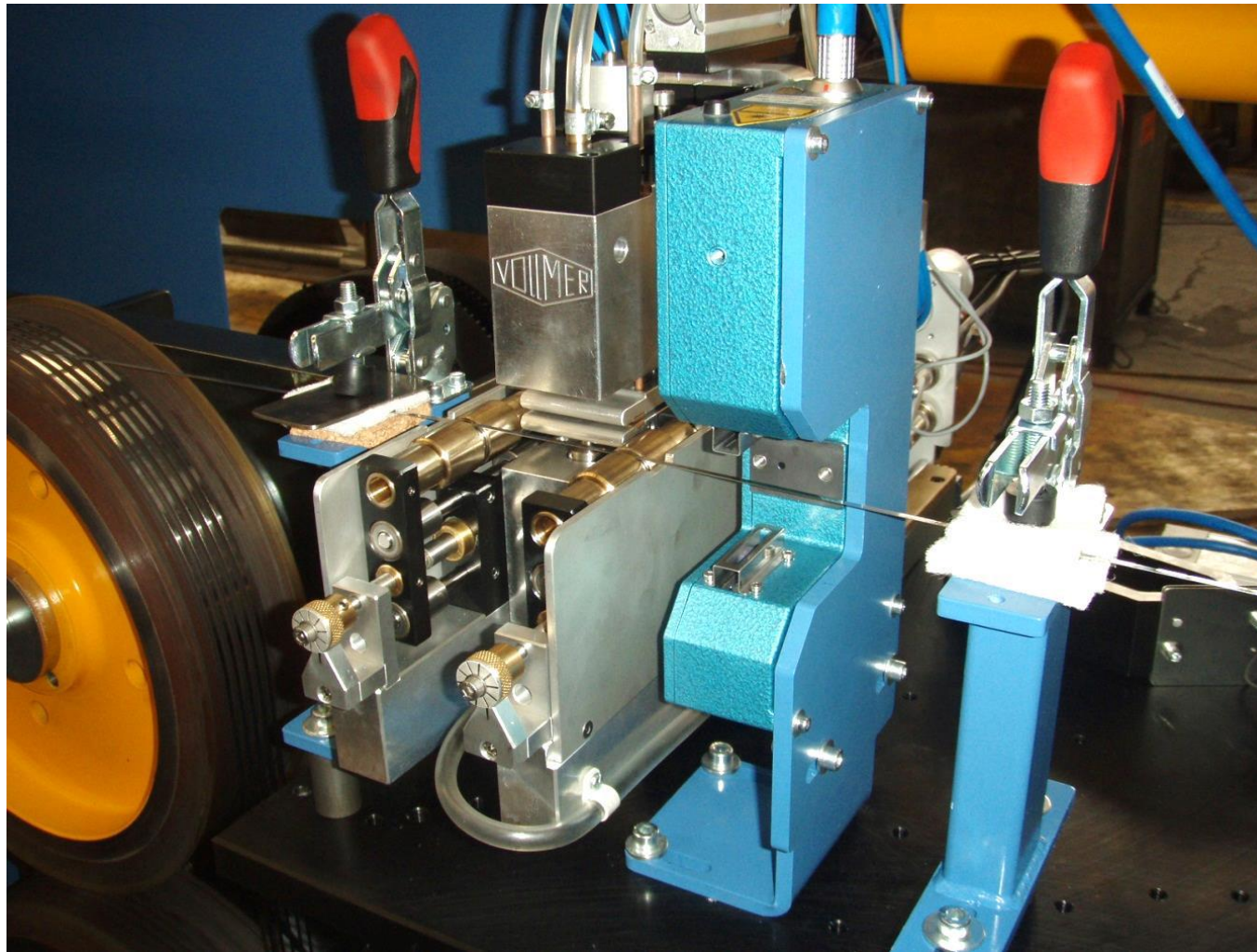
## PROFILEMASTER® PMM 80-4K

Profile measurement systems for drawn steel and non-ferrous profiles



## ODAC® 16-30

Laser scanning measurement system for flat wire



# 3 x ODAC® 151J

## Straightness measurement and monitoring system



## STEELMASTER SMS 100-S6

6-axes laser scanning measurement system for cold steel applications



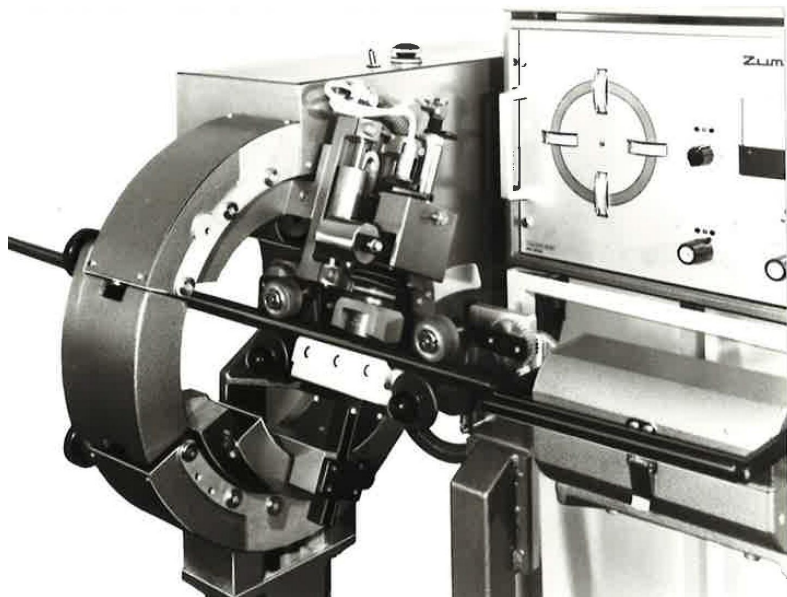
# PROFILEMASTER® SPS 400-S4

8-axes laser line triangulation system for hot steel application



# Focus on mechanical design, 60's

Eccentricity measurement systems





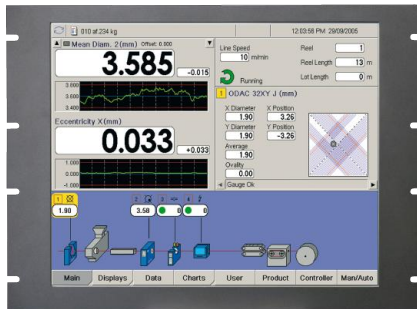
# Focus on electronics design, 80's

Electronics for diameter processing



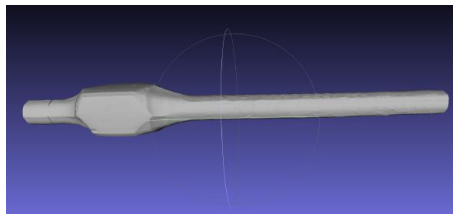
# Focus on software design, 90'

USYS computing system for fast data processing and higher-level functions



# Focus on applied mathematics, today

SPS for the measurement of profile in hot steel applications



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Implementation issues

# The RAYEX<sup>®</sup> S system

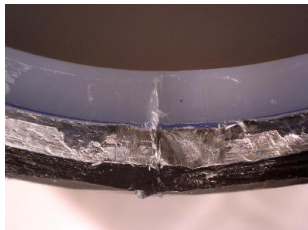
X-ray measurement system with two measurement axes



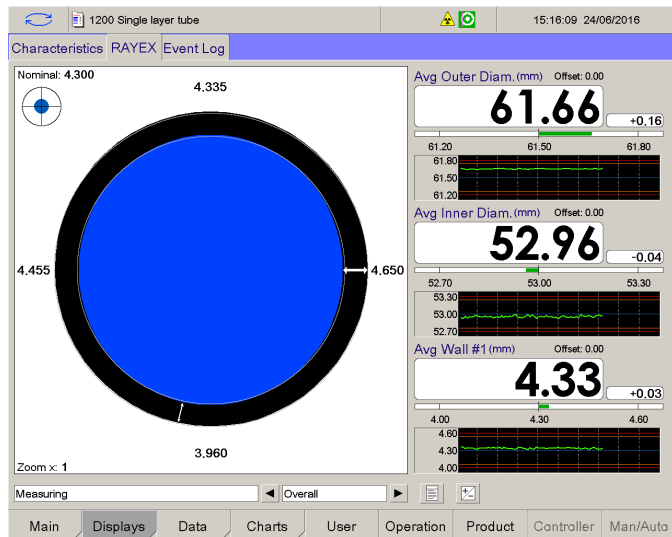
# The applications

Layer thickness and eccentricity in

- ▶ hoses
- ▶ tubes
- ▶ cables (jacketing)

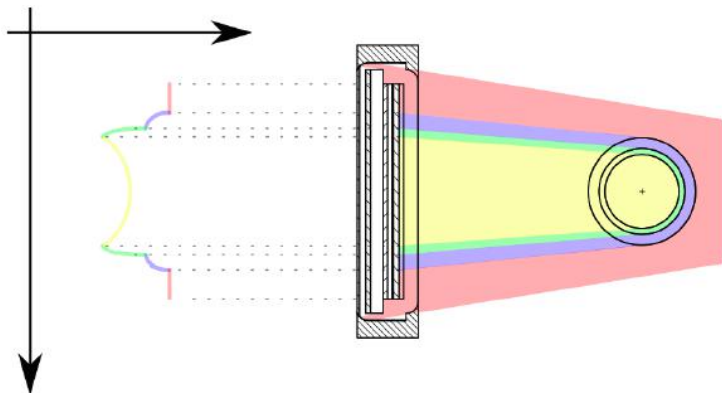


# Processing and display of measured values



## Measurement principle

Projection of two fan beams on line sensors: example of a two layer tube





# Specifications

- ▶ Accuracy 10  $\mu\text{m}$  (pixel width 50 $\mu\text{m}$ !)
- ▶ Sample rate  $> 10\text{Hz}$ 
  - ▶ faster=more robust against object motions,
  - ▶ slower=lower emissions
- ▶ Measurement of thickness of multilayer tubes (up to 3 layers)
- ▶ Measurement of cable jackets
- ▶ Robustness of measurement

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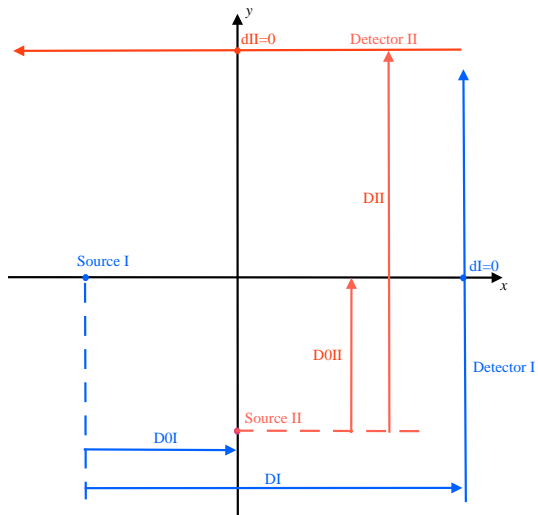
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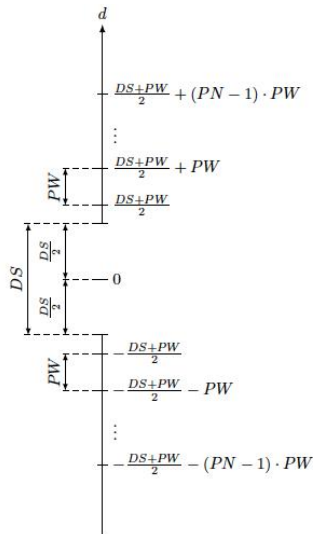
The IEFK for RAYEX<sup>®</sup> S

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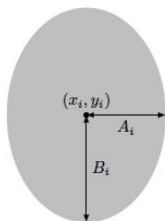
# Axes



# Detector geometry



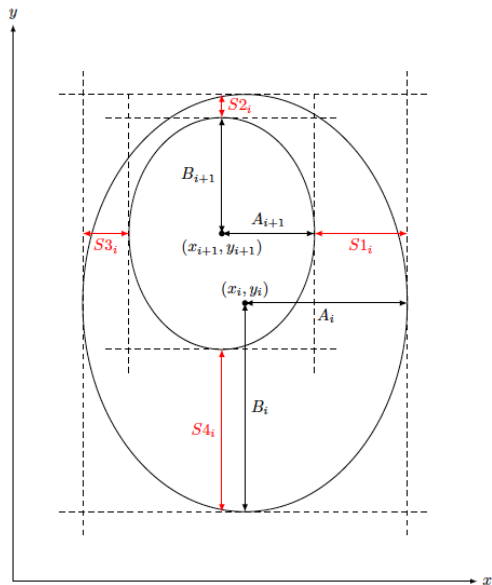
## Device under test (DUT)



Chord length is

$$c_i(d) = \frac{2 \cdot A_i \cdot B_i}{a_x^2(d) \cdot A_i^2 + a_y^2(d) \cdot B_i^2} \cdot \sqrt{a_x^2(d) \cdot A_i^2 + a_y^2(d) \cdot B_i^2 - (b(d) + a_x(d) \cdot x_i + a_y(d) \cdot y_i)^2}$$

# DUT with multiple layers



## X-ray beam

Beer-Lambert absorption law: beam intensity decays exponentially with chord length in material:

$$I(d) = I_0(d) \cdot e^{-K_i \cdot c_i(d)}$$

or also

$$(Abs_i(d)) = \ln \left( \frac{I(d)}{I_0(d)} \right) = -K_i \cdot c_i(d)$$

and

$$Abs(d) = \sum_i -K_i \cdot c_i(d)$$

## Detector sensitivity

- ▶ Thermal noise causes signal to be roughly proportional to exposure time (*Dark*)
- ▶ Full exposure may present different levels for each sensor/pixel (*Ref*)

Given measurement signal *Raw*, the normalized relationship for the intensity is

$$e^{Abs(d)} = \frac{I(d)}{I_0(d)} = \frac{Raw(d) - Dark(d)}{Ref(d) - Dark(d)}$$



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# Kalman filter (KF)

Given is a linear system are state-equation and output equation

$$\begin{aligned}\mathbf{x}_k &= \mathbf{F} \cdot \mathbf{x}_{k-1} + \mathbf{G} \cdot \mathbf{u}_{k-1} + \mathbf{w}_{k-1} \\ \mathbf{y}_k &= \mathbf{H} \cdot \mathbf{x}_k + \mathbf{v}_k\end{aligned}$$

with state vector  $\mathbf{x}_k$ , input  $\mathbf{u}_k$  and output  $\mathbf{y}_k$

State covariance matrix is

$$\mathbf{P}_k = \text{Cov}(\mathbf{x}_k, \mathbf{x}_k) = \mathbb{E} \left( (\mathbf{x}_k - \hat{\mathbf{x}}_k) \cdot (\mathbf{x}_k - \hat{\mathbf{x}}_k)^T \right)$$

## Noise model

Process noise  $\mathbf{w}_k$  and measurement noise  $\mathbf{v}_k$  assumed to have zero mean normal distributions:

$$\mathbf{w}_k \sim \mathcal{N}(0, \mathbf{Q}_k)$$

$$\mathbf{v}_k \sim \mathcal{N}(0, \mathbf{R}_k)$$

where  $\mathbf{Q}_k$  is process noise covariance matrix,  $\mathbf{R}_k$  measurement noise covariance matrix:

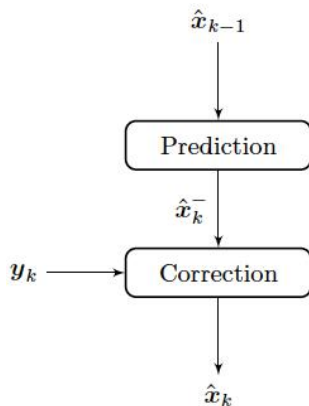
$$\mathbf{Q}_k = \text{Cov}(\mathbf{w}_k, \mathbf{w}_k) = \mathbb{E}(\mathbf{w}_k \cdot \mathbf{w}_k^T)$$

$$\mathbf{R}_k = \text{Cov}(\mathbf{v}_k, \mathbf{v}_k) = \mathbb{E}(\mathbf{v}_k \cdot \mathbf{v}_k^T)$$

# KF filter steps

Two step estimation

- ▶ first estimation with prediction of new output based on model and on current input (pre-estimate)
- ▶ second estimation with correction of pre-estimate with current measurement value (post-estimate)



# KF equations

## Prediction

Predict State Estimate

$$\hat{\mathbf{x}}_k^- = \mathbf{F}_{k-1} \cdot \hat{\mathbf{x}}_{k-1} + \mathbf{G} \cdot \mathbf{u}_{k-1}$$

Predict Error Covariance

$$\mathbf{P}_k^- = \mathbf{F}_{k-1} \cdot \mathbf{P}_{k-1} \cdot \mathbf{F}_{k-1}^\top + \mathbf{G}_{k-1} \cdot \mathbf{Q}_{k-1} \cdot \mathbf{G}_{k-1}^\top$$

## Correction

Compute Kalman Gain

$$\mathbf{K}_k = \mathbf{P}_k^- \cdot \mathbf{H}_k^\top \cdot (\mathbf{H}_k \cdot \mathbf{P}_k^- \cdot \mathbf{H}_k^\top + \mathbf{V}_k \cdot \mathbf{R}_k \cdot \mathbf{V}_k^\top)^{-1}$$

Correct State Estimate

$$\hat{\mathbf{x}}_k = \hat{\mathbf{x}}_k^- + \mathbf{K}_k \cdot (\mathbf{y}_k - \mathbf{H}_k \cdot \hat{\mathbf{x}}_k^-)$$

Correct Error Covariance

$$\mathbf{P}_k = (\mathbf{I} - \mathbf{K}_k \cdot \mathbf{H}_k) \cdot \mathbf{P}_k^-$$

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## Kalman filter states

Linear state transformation: Layer thicknesses as state variables

$$S1_i = A_i - A_{i+1} + x_i - x_{i+1}$$

$$S2_i = B_i - B_{i+1} + y_i - y_{i+1}$$

$$S3_i = A_i - A_{i+1} - x_i + x_{i+1}$$

$$S4_i = B_i - B_{i+1} - y_i + y_{i+1}$$

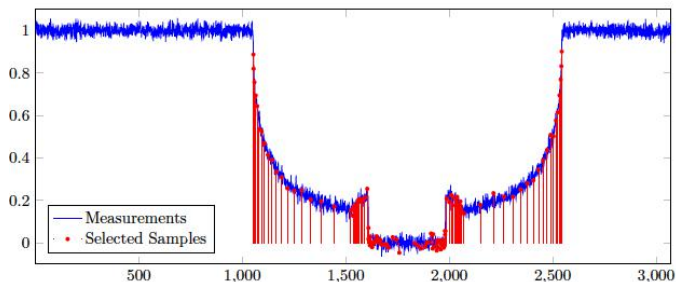
gives state

$$\mathbf{x} = [A_1, B_1, x_1, y_1, \mathbf{K}_{1,A,N}, S1_1, S2_1, S3_1, S4_1, \mathbf{K}_{2,A,N}, \dots, \\ S1_{I-1}, S2_{I-1}, S3_{I-1}, S4_{I-1}, \mathbf{K}_{I,N}, \Delta x, \Delta y]$$

## Sample measurement selection

Each CCD detector has two sets of 1536 pixels. Processing of 6144 pixels per sample is not practical.

⇒ Selection of representative pixels.





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**Implementation issues**

# Software implementation

- ▶ Development under Scilab (Matlab-like tool) and Embarcadero with C++
- ▶ Run-time environment Windows PC
- ▶ Encapsulation of Scilab code in wrapper within C++-code
- ▶ Functionally equivalent implementation of Scilab algorithm in C++

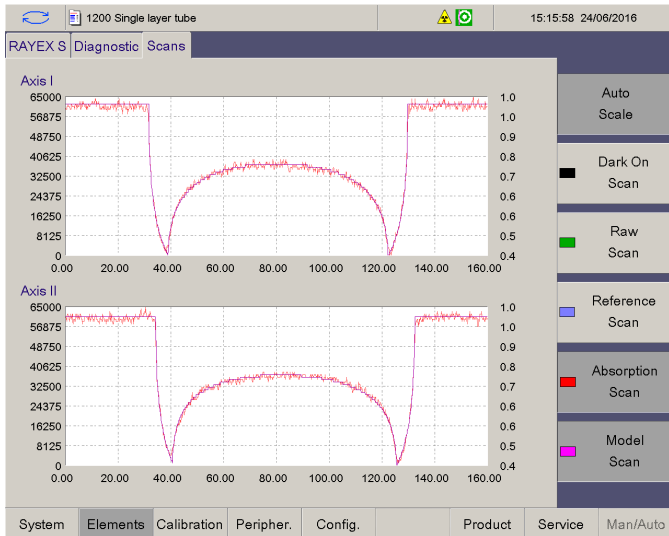
## Other mathematical issues dealt with

- ▶ Calibration of device and detector geometry
- ▶ Detector offset drift to be compensated on-line
- ▶ Object motion considered in Kalman filter
- ▶ Limited stability of x-ray source intensity (still open issue)
- ▶ and more ...

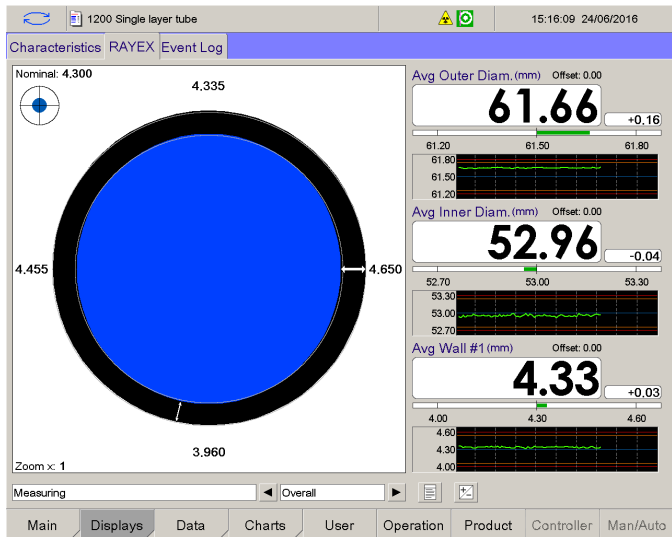
# Challenges

- ▶ Computational requirement to be minimized (wish of highest possible measurement rate)
- ▶ Simple operation (e.g. user should not define starting values for state)
- ▶ Limited complexity allowed on site (e.g. for calibration)
- ▶ Relevant environment uncertainties
- ▶ Strong object variability
- ▶ Non-ideal measurement process behavior (noise level drift, noise dynamics, material-dependent behavior)

# Profile for diagnostics



# Processing and display of measured values



Thank you for the attention!

Questions?