### Offline Reinforcement Learning

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### What makes modern machine learning work?









### What about reinforcement learning?



Mnih et al. '13



Schulman et al. '14 & '15



Levine\*, Finn\*, et al. '16





enormous gulf







### Can we develop **data-driven** RL methods?



Levine, Kumar, Tucker, Fu. Offline Reinforcement Learning: Tutorial, Review, and Perspectives on Open Problems. '20



# Why is offline RL difficult?



## How do we design offline RL algorithms?

Conservative Q-Learning

Model-based offline RL



How do we evaluate offline RL methods?



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## On-policy, off-policy, and offline RL

"Classic" RL diagram:



#### More typical use case:

This is a very **online** view of RL

on-policy RL



off-policy RL







### The RL objective



$$\underbrace{p_{\theta}(\mathbf{s}_{1}, \mathbf{a}_{1}, \dots, \mathbf{s}_{T}, \mathbf{a}_{T})}_{p_{\theta}(\tau)} = p(\mathbf{s}_{1}) \prod_{t=1}^{T} \pi_{\theta}(\mathbf{a}_{t} | \mathbf{s}_{t}) p(\mathbf{s}_{t+1} | \mathbf{s}_{t}, \mathbf{a}_{t})$$

it is very hard to optimize this with off-policy data directly  $\theta^{\star} = \arg \max_{\theta} E_{\tau \sim p_{\theta}(\tau)} \left[ \sum_{t} \gamma^{t} r(\mathbf{s}_{t}, \mathbf{a}_{t}) \right]$ 

### The RL objective



Aside: recovering the policy could optimize the above objective w.r.t.  $\pi_{\theta}$  directly  $\pi(\mathbf{a}_t | \mathbf{s}_t) = \begin{cases} 1 \text{ if } \mathbf{a}_t = \arg \max_{\mathbf{a}_t} Q^{\pi}(\mathbf{s}_t, \mathbf{a}_t) & \text{"greedy" policy} \\ 0 \text{ otherwise} & \text{can recover with optimization (e.g., CEM)} \end{cases}$ 

### The Q-function

$$Q^{\pi}(\mathbf{s}_{t}, \mathbf{a}_{t}) = E\left[\sum_{t'=t}^{\infty} \gamma^{t'-t} r(\mathbf{s}_{t'}, \mathbf{a}_{t'})\right] = r(\mathbf{s}_{t}, \mathbf{a}_{t}) + \gamma \left[r(\mathbf{s}_{t+1}, \mathbf{a}_{t+1})\right] + \gamma E\left[r(\mathbf{s}_{t+1}, \mathbf{a}_{t+2})\right] \dots$$
expectation under  $\pi_{\theta}(\mathbf{a}_{t}|\mathbf{s}_{t})$ 

$$Q^{\pi}(\mathbf{s}_{t+1}, \mathbf{a}_{t+1})$$

$$Q^{\pi}(\mathbf{s}_{t+1}, \mathbf{a}_{t+1})$$



**Bellman** equation:

$$Q^{\pi}(\mathbf{s}_t, \mathbf{a}_t) = r(\mathbf{s}_t, \mathbf{a}_t) + \gamma E[Q^{\pi}(\mathbf{s}_{t+1}, \mathbf{a}_{t+1})]$$

let's say we have a trajectory  $\mathbf{s}_1, \mathbf{a}_1, \mathbf{s}_2, \mathbf{a}_2, ..., \mathbf{s}_T, \mathbf{a}_T$ generated by some *other* policy  $\pi_\beta$ can we *estimate* the Bellman equation?

these come from our trajectory this is sampled from  $\pi_{\theta}$  $Q^{\pi}(\mathbf{s}_{t}, \mathbf{a}_{t}) \approx r(\mathbf{s}_{t}, \mathbf{a}_{t}) + \gamma Q^{\pi}(\mathbf{s}_{t+1}, \mathbf{a}_{t+1})$ 

this is a **single sample** estimate of the expectation

## The Q-function

these come from our trajectory this is sampled from  $\pi_{\theta}$  $Q^{\pi}(\mathbf{s}_{t}, \mathbf{a}_{t}) \approx r(\mathbf{s}_{t}, \mathbf{a}_{t}) + \gamma Q^{\pi}(\mathbf{s}_{t+1}, \mathbf{a}_{t+1})$ 



## Off-policy RL summary

 $Q(\mathbf{s}, \mathbf{a}) \leftarrow r(\mathbf{s}, \mathbf{a}) + E_{\mathbf{a}'}[Q(\mathbf{s}', \mathbf{a}')] \longleftarrow \text{don't need on-policy data for this!}$ 

off-policy Q-learning:

1. collect dataset  $\{(\mathbf{s}_i, \mathbf{a}_i, \mathbf{s}'_i, r_i)\}$  using some policy, add it to  $\mathcal{B}$ 

2. sample a batch  $(\mathbf{s}_i, \mathbf{a}_i, \mathbf{s}'_i, r_i)$  from  $\mathcal{B}$  $\cdots \cdots \sum (O(\mathbf{s}_i, \mathbf{a}_i) - [m(\mathbf{s}_i, \mathbf{a}_i) + E_i (O(\mathbf{s}'_i, \mathbf{a}'_i))])^2$ 

3. minimize 
$$\sum_i (Q(\mathbf{s}_i, \mathbf{a}_i) - [r(\mathbf{s}_i, \mathbf{a}_i) + E_{\mathbf{a}'_i}[Q(\mathbf{s}'_i, \mathbf{a}'_i)]])^2$$

more typical use case:

: (s,a,s',r)

 $\pi_{\theta}(a|s)$ 

臮

Update  $\pi_{\theta} \quad Q_{\phi}$ 

p(s'|s,a) 2. Online Fine-tuning

Update

1. Offline Learning

- off-policy data - expert demos - prior runs of RL  $\mathcal{D} = \{(s, a, s', r)_j\}$ 



### An instantiation of this idea...



Kalashnikov, Irpan, Pastor, Ibarz, Herzong, Jang, Quillen, Holly, Kalakrishnan, Vanhoucke, Levine. QT-Opt: Scalable Deep Reinforcement Learning of Vision-Based Robotic Manipulation Skills

### Does it work?







Method	Dataset	Success	Failure
Offline QT-Opt	580k offline	87%	13%
Finetuned QT-Opt	580k offline + 28k online	96%	4%

Kalashnikov, Irpan, Pastor, Ibarz, Herzong, Jang, Quillen, Holly, Kalakrishnan, Vanhoucke, Levine. QT-Opt: Scalable Deep Reinforcement Learning of Vision-Based Robotic Manipulation Skills

### Even worse...



#### training on random(ized) offline data



training on demo data



## What's the problem?



### Hypothesis 2: Training data is not good

Usually not the case: behavioral cloning of best data does better!

Kumar, Fu, Tucker, Levine. Stabilizing Off-Policy Q-Learning via Bootstrapping Error Reduction. NeurIPS '19

### Distribution shift in a nutshell

Example empirical risk minimization (ERM) problem:

 $\theta \leftarrow \arg\min_{\theta} E_{\mathbf{x} \sim p(\mathbf{x}), y \sim p(y|\mathbf{x})} \left[ (f_{\theta}(\mathbf{x}) - y)^2 \right]$ 

given some  $\mathbf{x}^*$ , is  $f_{\theta}(\mathbf{x}^*)$  correct?

 $E_{\mathbf{x} \sim p(\mathbf{x}), y \sim p(y|\mathbf{x})} \left[ (f_{\theta}(\mathbf{x}) - y)^2 \right]$  is low  $E_{\mathbf{x} \sim \bar{p}(\mathbf{x}), y \sim p(y|\mathbf{x})} \left[ (f_{\theta}(\mathbf{x}) - y)^2 \right]$  is not, for general  $\bar{p}(\mathbf{x}) \neq p(\mathbf{x})$ what if  $\mathbf{x}^* \sim p(\mathbf{x})$ ? not necessarily...

usually we are not worried – neural nets generalize well!

what if we pick  $\mathbf{x}^{\star} \leftarrow \arg \max_{\mathbf{x}} f_{\theta}(\mathbf{x})$ ?



### Where do we suffer from distribution shift?

$$Q(\mathbf{s}, \mathbf{a}) \leftarrow r(\mathbf{s}, \mathbf{a}) + \max_{\mathbf{a}'} Q(\mathbf{s}', \mathbf{a}')$$

$$Q(\mathbf{s}, \mathbf{a}) \leftarrow r(\mathbf{s}, \mathbf{a}) + E_{\mathbf{a}' \sim \pi_{new}}[Q(\mathbf{s}', \mathbf{a}')]$$

$$y(\mathbf{s}, \mathbf{a})$$

what is the objective?



Kumar, Fu, Tucker, Levine. Stabilizing Off-Policy Q-Learning via Bootstrapping Error Reduction. NeurIPS '19



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How do we evaluate offline RL methods?

### How do prior methods address this?

$$= \pi_{\text{new}}(\mathbf{a}|\mathbf{s}) = \arg\max_{\pi} E_{\mathbf{a} \sim \pi(\mathbf{a}|\mathbf{s})}[Q(\mathbf{s},\mathbf{a})] \text{ s.t. } D_{\text{KL}}(\pi \| \pi_{\beta}) \le \epsilon$$

This solves distribution shift, right?

No more erroneous values?

**Issue 1:** Estimating the behavior policy is difficult

Issue 2: This might be too conservative (we'll come back to this) "policy constraint" method

very old idea (but it had no single name?)

Todorov et al. [passive dynamics in linearlysolvable MDPs]

Kappen et al. [KL-divergence control, etc.]

trust regions, covariant policy gradients, natural policy gradients, etc.

used in some form in recent papers: Fox et al. '15 ("Taming the Noise...") Fujimoto et al. '18 ("Off Policy...") Jaques et al. '19 ("Way Off Policy...") Kumar et al. '19 ("Stabilizing...") Wu et al. '19 ("Behavior Regularized...")

## When is estimating the behavior policy hard?

**Issue 1:** Estimating the behavior policy is difficult

### > Easy case: all data comes from the same Markovian policy

• This is not very common or realistic

### Hard case: data comes from many different policies

- Very common in reality (e.g., some demo data from humans, some scripted data)
- Very common during *online finetuning*



### Avoiding behavior policies with **implicit** constraints

Peng\*, Kumar\*, Levine. Advantage-Weighted Regression. '19

Nair, Dalal, Gupta, Levine. Accelerating Online Reinforcement Learning with Offline Datasets. '20



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### What about those Q-value errors?



$$\hat{Q}^{\pi} = \arg\min_{Q} \max_{\mu} \alpha E_{\mathbf{s} \sim D, \mathbf{a} \sim \mu(\mathbf{a}|\mathbf{s})} [Q(\mathbf{s}, \mathbf{a})]$$
 term to push down big Q-values regular objective  $-\left\{ +E_{(\mathbf{s}, \mathbf{a}, \mathbf{s}') \sim D} \left[ (Q(\mathbf{s}, \mathbf{a}) - (r(\mathbf{s}, \mathbf{a}) + E_{\pi}[Q(\mathbf{s}', \mathbf{a}')]))^2 \right]$ 

can show that 
$$\hat{Q}^{\pi} \leq Q^{\pi}$$
 for large enough  $\alpha$   
 $\uparrow$   
true Q-function

### Learning with Q-function lower bounds

A better bound: <u>always</u> pushes Q-values down push <u>up</u> on (**s**, **a**) samples in data  $\hat{Q}^{\pi} = \arg \min_{Q} \max_{\mu} \alpha E_{\mathbf{s} \sim D, \mathbf{a} \sim \mu(\mathbf{a}|\mathbf{s})} [Q(\mathbf{s}, \mathbf{a})] - \alpha E_{(\mathbf{s}, \mathbf{a}) \sim D} [Q(\mathbf{s}, \mathbf{a})] + E_{(\mathbf{s}, \mathbf{a}, \mathbf{s}') \sim D} \left[ (Q(\mathbf{s}, \mathbf{a}) - (r(\mathbf{s}, \mathbf{a}) + E_{\pi}[Q(\mathbf{s}', \mathbf{a}')]))^2 \right]$ 

no longer guaranteed that  $\hat{Q}^{\pi}(\mathbf{s}, \mathbf{a}) \leq Q^{\pi}(\mathbf{s}, \mathbf{a})$  for all  $(\mathbf{s}, \mathbf{a})$ 

but guaranteed that  $E_{\pi(\mathbf{a}|\mathbf{s})}[\hat{Q}^{\pi}(\mathbf{s},\mathbf{a})] \leq E_{\pi(\mathbf{a}|\mathbf{s})}[Q^{\pi}(\mathbf{s},\mathbf{a})]$  for all  $\mathbf{s} \in D$ 

Kumar, Zhou, Tucker, Levine. Conservative Q-Learning for Offline Reinforcement Learning. '20



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### How does **model-based** RL work?

... so the model's predictions are invalid

these states are OOD



the model answers "what if" questions

 $\hat{p}(\mathbf{s}_{t+1}|\mathbf{s}_t,\mathbf{a}_t)$ 



what goes wrong when we can't collect more data?



### MOPO: Model-Based Offline Policy Optimization

solution: "punish" the policy for exploiting

$$\tilde{r}(\mathbf{s}, \mathbf{a}) = r(\mathbf{s}, \mathbf{a}) - \lambda u(\mathbf{s}, \mathbf{a})$$
  
uncertainty penalty

...and then use any existing model-based RL algorithm



Yu\*, Thomas\*, Yu, Ermon, Zou, Levine, Finn, Ma. **MOPO: Model-Based Offline Policy Optimization.** '20 See also: Kidambi et al., **MOReL : Model-Based Offline Reinforcement Learning.** '20 (concurrent)

### MOPO: Theoretical Analysis

 $\tilde{r}(\mathbf{s}, \mathbf{a}) = r(\mathbf{s}, \mathbf{a}) - \lambda u(\mathbf{s}, \mathbf{a})$ 



 $\eta_M(\hat{\pi}) \ge \eta_M(\pi^\star) - 2\lambda\epsilon_u(\pi^\star)$ 

> quantifies "optimality gap" in terms of model error

Yu\*, Thomas\*, Yu, Ermon, Zou, Levine, Finn, Ma. MOPO: Model-Based Offline Policy Optimization. '20

### COMBO: Conservative Model-Based RL

Basic idea: just like CQL minimizes Q-value of policy actions, we can minimize Q-value of model state-action tuples

state-action tuples from the model

$$\hat{Q}^{k+1} \leftarrow \arg\min_{Q} \beta \left( \mathbb{E}_{\mathbf{s}, \mathbf{a} \sim \rho(\mathbf{s}, \mathbf{a})} [Q(\mathbf{s}, \mathbf{a})] - \mathbb{E}_{\mathbf{s}, \mathbf{a} \sim \mathcal{D}} [Q(\mathbf{s}, \mathbf{a})] \right) \\ + \frac{1}{2} \mathbb{E}_{\mathbf{s}, \mathbf{a}, \mathbf{s}' \sim d_f} \left[ \left( Q(\mathbf{s}, \mathbf{a}) - \widehat{\mathcal{B}}^{\pi} \widehat{Q}^k(\mathbf{s}, \mathbf{a})) \right)^2 \right].$$
(4)

**Intuition:** if the model produces something that looks clearly different from real data, it's easy for the Q-function to make it look bad

Dataset type	Environment	BC	COMBO (ours)	MOPO	CQL	SAC-off	BEAR	BRAC-p	BRAC-v
random	halfcheetah	2.1	38.8	35.4	35.4	30.5	25.1	24.1	31.2
random	hopper	1.6	17.9	11.7	10.8	11.3	11.4	11.0	12.2
random	walker2d	9.8	7.0	13.6	7.0	4.1	7.3	-0.2	1.9
medium	halfcheetah	36.1	54.2	42.3	44.4	-4.3	41.7	43.8	46.3
medium	hopper	29.0	94.9	28.0	86.6	0.8	52.1	32.7	31.1
medium	walker2d	6.6	75.5	17.8	74.5	0.9	59.1	77.5	81.1
medium-replay	halfcheetah	38.4	55.1	53.1	46.2	-2.4	38.6	45.4	47.7
medium-replay	hopper	11.8	73.1	67.5	48.6	3.5	33.7	0.6	0.6
medium-replay	walker2d	11.3	56.0	39.0	32.6	1.9	19.2	-0.3	0.9
med-expert	halfcheetah	35.8	90.0	63.3	62.4	1.8	53.4	44.2	41.9
med-expert	hopper	111.9	111.1	23.7	111.0	1.6	96.3	1.9	0.8
med-expert	walker2d	6.4	96.1	44.6	<b>98.7</b>	-0.1	40.1	76.9	81.6



#### Yu, Kumar, Rafailov, Rajeswaran, Levine, Finn. COMBO: Conservative Offline Model-Based Policy Optimization. 2021.



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typical protocol in prior work:

- 1. train  $\pi_{\beta}$  with online RL
- 2. either collect data throughout training OR
- 2. collect data from final policy  $\pi_{\beta}$

### this is a really bad idea

- If you already have a good policy, why bother with offline RL?
- In the real world, data might come from non-Markovian "policies"
  - Human users
  - Hand-engineered policies
- Must use data that is representative of real-world settings and leaves lots of room for improvement
- Offline RL must learn policies that are much better than the behavior policy!

without testing these properties, we **cannot** trust that our algorithms are good!

## D4RL: Datasets for Data-Driven Deep RL

What are some important principles to keep in mind?

Data from non-RL policies, including data from humans

**Stitching:** data where dynamic programming can find much better solutions



**Realistic tasks** 







simulation & human data from Rajeswaran et al.

Fu, Kumar, Nachum Tucker, Levine. D4RL: Datasets for Data-Driven Deep Reinforcement Learning. '20



Kumar, Zhou, Tucker, Levine. Conservative Q-Learning for Offline Reinforcement Learning. '20

## Which offline RL method should I use?

#### **AWR-like methods CQL-like methods** seems to get best results on external seems to get best results on external these are purely benchmarks (e.g., D4RL) benchmarks when finetuning empirical observations, and they might change from my experience, harder to use with seems to be much worse than CQL on with better online finetuning (too conservative) benchmarks (e.g., D4RL) in fully offline mode implementations! modifies the critic modifies the actor seems to imply we can combine to get the best of both worlds we have not been successful at this so far

## Summary and takeaways

- Offline RL algorithms can be built out of Q-Learning methods
- But this can fail if there is narrow coverage (often the case in IL+RL)
- > Offline RL is difficult because of **distributional shift**
- Solutions typically mitigate this in some way
- AWR & AWAC: implicit constraint formed by using a weighted imitation learning objective (weighted using the critic!)
- CQL: conservative critic objective that directly avoids overestimation
- Model-based offline RL: similar principle, avoid overestimating by penalizing value far from data



how well it does

 $\mathbf{X}$ 

how well it thinks

it does (Q-values)